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ABSTRACT

The Warren Abstract Machine (WAM) has become a generally accepted standard Prolog implementation technique. Garbage collection is an important aspect in the implementation of any Prolog system. We first present a synopsis of the WAM and then show marking and compaction algorithms that take advantage of WAM's unique use of the data areas. Marking and compaction are performed on both the heap and the trail. The marking and compaction algorithms use pointer reversal techniques, which obviate the need for extra stack space. However, two bits for every pointer on the heap are reserved for the garbage collection algorithm. The algorithm can work on segments of the heap, which may lead to a significant reduction of the total garbage collection time. The time of the algorithms are linear in the size of the areas.

Introduction

A variety of techniques, such as tail recursion optimization, have been developed in an effort to minimize memory consumption. However none of these techniques have reduced the amount of garbage substantially enough to reduce the rôle of garbage collection in Prolog. In developing an algorithm one must keep in mind that the heap is used in a stack fashion; it grows during forward execution and is unwound during backtracking. This requires a garbage collection algorithm that maintains the order of data created on the heap.

The main algorithms in this paper are linear, requiring two bits per word of pointer storage. The ideas of segmented garbage collection [Lieberman 83, Pittomvils 85], are incorporated in the design. The algorithms are for use by a single processor system.

The rest of the paper is organized as follows: First a synopsis of Warren's Prolog implementation, the Warren Abstract Machine (WAM), is given. We then describe a general marking and compaction algorithm. As a first optimization of the algorithm, we show how to use the trail information to increase the amount of detectable garbage and to be able to compact the trail. Thereafter we discuss segmented garbage collection, a method for reducing the search space.

Synopsis of the WAM

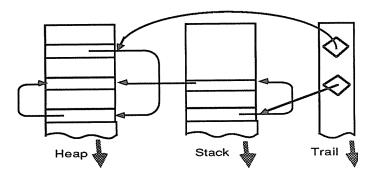
In 1983, Warren published a description of an abstract machine for Prolog execution [Warren 83]. The paper describes an instruction set and several data areas that the instructions operate on. The instructions are oriented towards the source language rather than towards the target machine. Thus an abstract instruction usually corresponds to a source program symbol but may involve a large, even unbounded, number of machine operations.

Warren's instruction set has since become generally accepted as the standard Prolog implementation technique and has been realized both by bytecode emulators, compilation into native instructions, and emulation in firmware and hardware. We shall not contemplate these techniques further.

Several authors have described optimized or extended versions of the WAM. The rest of this chapter contains a condensed description of a somewhat simplified WAM. For instance, we do not treat all instructions, nor their complete semantics. A more detailed description of WAM may be found in [Gabriel 84, WarrenDS 84].

Data areas

The data areas are the *code area*, containing the program itself, the *control area*, containing the abstract machine registers, and three areas operated as stacks: The *(local) stack* contains information pertaining to backtracking and recursive procedure invocations. The *global stack* or *heap* contains structures, lists, and value cells created by Prolog execution. The *trail stack* contains references to conditionally bound variables, i.e. it records such bindings that have to be undone upon backtracking.



The stack is assumed to grow in the positive direction, towards higher addresses, which is downwards in our figures. The first cell of the heap, the stack and the trail are called heap_low, stack_low and trail_low respectively.

The heap

An important concept is that of a *value cell*. A value cell stores a Prolog term and consists of a *tag*, a *value*, and two *bits* used in garbage collection. The heap consists exclusively of value cells. There are value cells on the stack as well. The following rules govern how value cells may refer to one another:

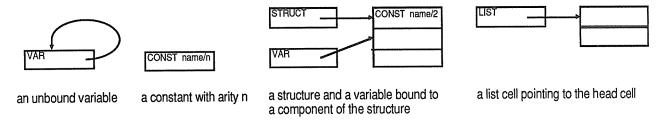
- A heap cell may only refer to another heap cell.
- · A stack cell may refer to an earlier stack cell or to a heap cell.

A possible pseudo-C declaration for value cells could be:

```
struct valuecell {
    int tag:2;
    struct valuecell *value:28;
    bool m:1;
    bool f:1;
};
```

During the marking phase, the m bit is set for the marked value cells, whereas the f bit distinguishes the first cell of a structure or list. Both bits are initially FALSE. The tag distinguishes the type of the term, the main types being references (VAR), structures (STRUCT), lists (LIST), and constants (CONST). An unbound variable is represented as a reference to itself. A value cell tagged as a variable but not pointing to itself represents a bound variable. Structures are created by explicitly copying the functor and arguments into consecutive value cells on the heap. The

value part of the functor value cell encodes its function symbol f and arity n. Functors are written as f/n. Lists are created similarly, except no functor needs to be stored. This technique for creating structures and lists is known as structure copying. For constants, the value field refers to something outside the scope of garbage collection. That is, the cell either points to a static area or contains a static value, e.g. an integer. In any case, the contents of the cell is ignored by garbage collection. We depict the different types of terms as follows:



Note that a variable may point at an individual element of a list or structure, but may not point at the first component of a structure, i.e. at the functor.

The control area

This area consists of pointers into the other areas plus a scratchpad register bank for passing arguments and for temporary usage. The contents of the control area registers defines the computation state. In the rest of this paper, we shall in fact treat the control area registers as if they were globally accessible machine registers. Indeed, that is how they are typically implemented.

where m is a suitable number defining the arity limit of functors and predicates.

A few words about C syntax and semantics:

The declaration struct wam *B; means that B is a pointer to a saved WAM state. Since B is such a pointer, then B->P is the P component of that structure. The declaration struct valuecell **T; means that T is a pointer to a pointer to a valuecell. Dereferencing one step is done by *T, which is just a pointer to a valuecell.

There are two more items which are used over short sequences of instructions.

```
struct valuecell *S;  /* current structure */
bool RW:1;  /* read or write mode bit */
```

However, these are never valid when garbage collection occurs, and so are not included in the "struct wam" definition.

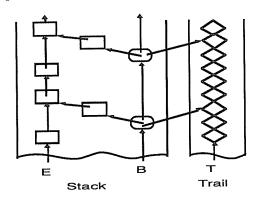
The local stack

The local stack contains two kinds of structures: *environments* and *choice points*. An environment represents a list of goals still to be executed. It consists of a number k of local variables occurring in the body of a clause plus a pointer into the body of a continuation clause and its environment. A local variable may be unbound, in which case it points to itself just like unbound heap variables. Unbound variables on the stack save heap storage but complicate the instruction set somewhat. We ignore these complications in this description.

Environments are only needed for clauses with more than one body goal, and are established when entering such clauses. They are (logically) discarded before executing the last body goal. The format of an environment is:

An environment can be *active* or *inactive*. An active environment is in the current execution path, in which case it is in the chain formed by the CE fields. An inactive environment is one which is associated with a clause that has finished execution, but may be reactivated upon backtracking. In this case it is only reachable via a choice point. Since an environment refers to its parent environment and several environments may have the same parent, the environments form a tree which has one active leaf, E, and zero or more inactive leaves.

The following picture shows the tree structure of the stack and the trail. A rectangle denotes an environment whereas a rounded rectangle denotes a choice point. A diamond denotes a trail cell, which in turn points either to the stack or to the heap (not shown in this picture).



A choice point is established when entering a procedure Q with n arguments which has more than one clause that could match the goal. It consists of a snapshot of the control area. Thus the format of a choice point is a "struct wam", except the argument registers A contain a copy of the n arguments of Q, and the P component represents the next possibly matching clause. A choice point contains enough information for restoring the state of computation back to as it was when entering Q. When no more alternatives remain, the choice point is discarded.

All choice points form a list linked by the B fields.

Note that the top of local stack is not recorded explicitly. Instead, when an environment or a choice point is established, it is placed at the next free location, computed as:

```
max(B,E + env_size(L))
```

where env_size(L) refers to the second operand of the call instruction (see below) pointed to by the continuation program counter, as this indicates the size of the current environment. Thus a choice point "freezes" all existing structures on the local stack, preventing them from being physically deallocated or written over.

The trail

This area records *conditional* variable bindings. A variable is conditionally bound if and only if the variable is older than the latest choice point. For heap variables, WAM compares the address of the variable with the H field of the latest choice point. For stack variables, the address of the variable is compared with the address of the latest choice point i.e. with B. Upon backtracking, entries are simply popped off of the trail stack and the bound variables are reset to unbound.

Treatment of Variables

The abstract machine distinguishes two kinds of variables. A *permanent* variable is one that occurs in more than one body goal, counting the head as part of the first body goal. Thus a permanent variable has to be kept across one or more procedure calls, and so needs an environment slot. Slots are assigned in such a way that they can be discarded as early as possible: the permanent variable whose last occurrence is earliest will get the slot with the highest location.

Thus environments shrink by zero or more slots for each body goal, releasing local stack space piecewise rather than an environment at a time. This optimization is called "environment trimming" and generalizes tail recursion optimization.

A temporary variable is any variable not classified as permanent. Temporary variables temporarily hold data during unification and are used for passing arguments in procedure calls. Procedures do not need to preserve temporary variables.

Consider, for example, the clause

```
p(A,B,S0,S) := q(A,B,C,C), r(S0,S1), r(S1,S).
```

where A, B, and C are temporary and all other variables are permanent.

The instruction set

Prolog programs compile into sequences of instructions, approximately one instruction per Prolog symbol. Instructions can take up to two operands, identifying temporary variables (Xi), permanent variables (Yi), small integers (N), constants (C), functors (F), and procedures (P). The instruction set is classified into *get*, *put*, *unify*, *procedural*, and *indexing* instructions. We shall consider the following example when discussing the instruction set. For reasons of space, formal definitions of the instructions cannot be included.

```
#1: concatenate([],L,L).
#2: concatenate([X|L1],L2,[X|L3]) :- concatenate(L1,L2,L3).
```

A naïve assignment of temporary variables in clause #2 is to reserve X1-X3 for the arguments and X4-X7 for X, L1, L2, and L3, respectively. There are no permanent variables.

Get instructions

Get instructions correspond to head arguments. They match against the procedure's arguments, passed in argument registers:

```
get_variable Vn, Ai % Vn is assigned the value of Ai get_value Vn, Ai % The values of Vn and Ai are unified get_constant C, Ai % The value of Ai is unified with the constant C get_nil Ai % The value of Ai is unified with the constant [] get_structure F, Ai % The value of Ai is unified with the structure F(..) % The value of Ai is unified with a list
```

Here, Ai denotes an argument register which is just another name for a temporary variable. The abbreviation Vn denotes a permanent or temporary variable. The suffix (constant, list, etc.) suggests what the argument should match. The variable suffix stands for the first occurrence of a variable; value is used for subsequent occurrences.

The head arguments of clause #2 compile to:

```
% concatenate([
get list A1
unify_variable X4
                         응
                                           L1],
                         왕
unify variable X5
                         양
                                        L2,
get variable X6,A2
                                        [
                         용
get list A3
                                         XΙ
                         응
unify_value X4
                                           L3])
unify_variable X7
```

Put instructions

Put instructions correspond to body arguments. They load arguments into argument registers.

```
put_variable Vn, Ai % Vn and Ai are assigned a new variable
put_value Vn, Ai % Ai is assigned the value of Vn
put_constant C, Ai % Ai is assigned the constant C
put_nil Ai % Ai is assigned the constant []
put_structure F, Ai % Ai is assigned the structure F(..)
put list Ai % Ai is assigned a list
```

The arguments of the goal of clause #2 compile to:

Unify instructions

Unify instructions correspond to arguments of a list or structure, and operate in $read \ mode$ or $write \ mode$, as indicated by the RW bit. If Ai contains a structure with functor F/n, the instruction $get_structure \ F/n$, Ai will put WAM in read mode and set the S register pointing at the arguments. Following the get instruction, n unify instructions will match subterms accessed via the S register, running in read mode. If instead Ai contains an uninstantiated variable, the get instruction will bind this variable to a structure which is about to be created, place F/n at the top of the heap, and put WAM in write mode. The unify instructions will fill in the subterms, running in write mode.

The get_list instruction operates similarly. The put_structure and put_list instructions always put WAM in write mode.

```
read mode semantics
                             % Vn is assigned the next subterm
unify_variable Vn
                             % The value of Vn is unified with the next subterm
unify_value Vn
                             % The next subterm is unified with the constant C
unify_constant C
                             % The next subterm is unified with the constant []
unify nil
write mode semantics
                              % A new variable is stored in Vn and as the next subterm
unify variable Vn
                              % The value of Vn is stored as the next subterm
unify value Vn
                              % The constant C is stored as the next subterm
unify_constant C
                              % The constant [] is stored as the next subterm
unify nil
```

Note that there are no *unify* instructions for lists or structures, as they would require extensions to the WAM data areas or registers. Instead, structures are "flattened" by introducing temporary variables. For instance, a head

```
p([d(0,a)])
```

could compile to:

```
get_list Ai % p([
unify_variable Xj % T1
unify_nil % ]):-
get_structure d/2,Xj % T1 = d(
unify_constant 0 % 0,
unify_constant a % a)
```

As a goal, it could compile to:

```
put_structure d/2,Xj % T1 = d(
unify_constant 0 % 0,
unify_constant a % a),
put_list Ai % p([
unify_value Xj % T1
unify_nil % T])
```

Procedural instructions

These instructions correspond to the head and goals of a clause. They deal with control transfer and environment handling:

```
proceed % branch to the continuation program pointer
execute Q
call Q,N % set the continuation program pointer at the next instruction,
% then branch to the procedure Q

allocate % establish an environment on the stack
deallocate % logically discard an environment
```

Clauses with zero, one, or more goals are translated according to the pattern:

```
F := G, H, K.
                             F :- G.
F.
                                                            allocate
                            get args of F
get args of F
                                                            get args of F
                            put args of G
proceed
                                                            put args of G
                             execute G
                                                             call G, N
                                                             put args of H
                                                             call H, N1
                                                             put args of K
                                                             deallocate
                                                             execute K
```

where $N \ge N1$ indicate the size of the part of the current environment which is active after the call instruction. Thus N permanent variables are live after the first call; N1 are live after the second call. It is this operand which is referred to as env_size(L) in the description of the local stack above.

Indexing instructions

For a given call, these instructions filter out the set of possibly matching clauses of a procedure. This function is based on the principal functor of the first argument. It is guaranteed that all possible matches can be eventually tried by backtracking. There are two kinds of indexing instructions: instructions that discriminate on the first argument:

and instructions that backtrack over alternatives:

```
try_me_else L % a new alternative program point is L
retry_me_else L % set alternative program point to L
trust_me_else_fail % discard latest alternative program point

try L % the next instruction is a new alternative program point, goto L
retry L % the next instruction replaces alternative program point, goto L
trust L % discard latest alternative program point, goto L
```

The clauses of concatenate/3 are linked together as follows:

```
switch_on_term $1,$2,$4,fail
$1: try_me_else $3
$2: /* the code for clause #1 */
$3: trust_me_else_fail
$4: /* the code for clause #2 */
```

The first instruction does a four-way dispatch on the type of the first argument: if it is a variable, both clauses are possible and so the try_me_else instruction establishes a choice point whose alternative label is \$3 before executing clause #1. If WAM backtracks, the trust_me_else_fail instruction will erase the choice point. If the first argument is respectively a constant or list, then the only possible alternatives are clause #1 or #2 (label \$2 or \$4), respectively. If it is a structure, the call fails.

The retry_me_else instruction is used for alternatives except the first and last ones.

The other switch instructions are used when there are several clauses with a constant or a structure as first head argument, respectively. These instructions provide further filtering of the set of possible matches by doing a hash table lookup with the principal functor as key.

The try/retry/trust instructions are used when there are several clauses with a first head argument with the same principal functor.

Compiler optimizations

There are several opportunities for compiler optimizations. For instance, the two instructions

```
get_variable Xj,Aj
put_value Xj,Aj
```

represent noops and can be deleted, and a compiler could try minimize the size of the emitted code by properly allocating temporary variables. Thus an optimized version of clause 2 above is:

```
% concatenate([
get list A1
                         용
                                         X |
unify variable X4
unify variable A1
                                           L1], L2,
                         용
get list A3
                         왕
unify value X4
                                           L3]) :-
                         왕
unify variable A2
                         % concatenate(L1,L2,L3).
execute concatenate/3
```

This version is four instructions shorter than the naïve translation given earlier.

Basic garbage collection algorithm

We first describe a rudimentary garbage collection algorithm, and in the subsequent sections we enhance it to take more advantage of the specific properties of Prolog. Our garbage collection algorithm consists of marking and compaction.

The marking phase

During this phase all reachable objects from a set of roots are marked by setting the m-bits of the value cells. The f-bit is initially FALSE but is temporarily used and reset to FALSE at the end of the marking phase.

Prerequisites for the marking phase

In the original WAM, some value cells on the stack may be uninitialized. A straightforward way to ensure that every environment is fully initialized at every procedure call requires the following changes in the WAM [Carlsson86]:

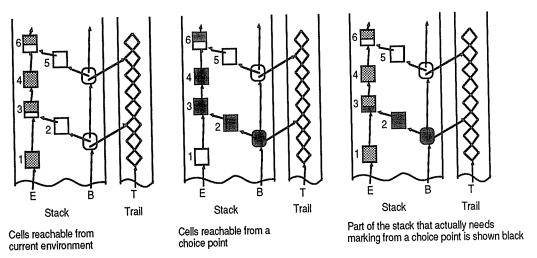
- All environment slots are initialized to unbound before the first call by inserting sufficient put variable Yn instructions.
- As a compensation we may optimize the WAM code after the first call by changing every put variable Yn into put_value Yn.
- In the body of a clause the semantics of unify_variable Yn are modified so that Yn is trailed if the computation is in a nondeterministic state. This will ensure that the variable will be reset on backtracking, thus avoiding the possibility of dangling references.

In the following we assume that garbage collection is triggered at a well defined point, for instance just after the call instruction. The arity of the predicate called indicates the number of active argument registers .

The marking algorithm

First all structures on the heap accessible from the active argument registers are marked. Since most computer architectures cannot handle a reference to a register and the mark_variable routine (defined later) takes a reference to a value cell, each register is first moved to the local variable temp. The notation &temp used below means the address of temp.

Then all active environments are marked. The environment size of E is computed as env_size(L).



In the first figure above, the chain of active environments reachable from the current environment E is marked, indicated by the shaded cells. From each choice point there is another chain of environments, as can be seen from the next figure. Some environments are only reachable from the choice point (2) and some are shared (3,4,6). The first shared environment (3) is a bit special: some cells within it may only be reachable from the chain starting at the choice point. Those cells are always the last cells allocated in that environment.

As illustrated by the third figure above, only a part of the active environment stack needs marking when accessed from a choice point. In our marking algorithm this optimization is implemented by first checking whether the given stack cell has already been marked, and in that case immediately stop marking that chain of environments. To make this work properly two observations have to be made:

- 1. The value cells of each environment have to be traversed from high to low, i.e. from the top of stack towards the bottom. By doing so, we will first encounter the possibly unmarked cells of a shared environment.
- 2. When marking a value cell on the stack, a reference within the stack is ignored. This is quite safe to do since WAM guarantees that all references within the stack are within the same chain of environments. Thus the referenced cell will be marked anyway.

The routine that marks a chain of environments is called mark_environments:

All choice points and the corresponding chains of environments are marked by mark_choicepoints:

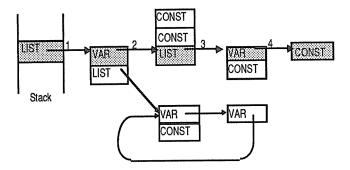
A note on the trail: Any variable recorded in the trail is also accessible from some choice point. Thus all variables reachable from the trail have already been marked and the trail need not be scanned. Later, in the section Early reset of variables, we will elaborate further on this subject.

Pittomvils et al. [Pittomvils 85] present a similar way to traverse the environments and the choicepoints, but give no details on how to mark the variables. Before we present the procedure mark_variable some background information on the marking phase is first given. Two concepts are of importance: chains and structures.

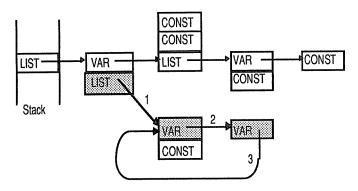
A chain is a linked list of valuecells. The cells of a chain are classified as follows. A head of chain is either a cell on the stack or any cell in a structure except the first one. A last cell of chain is either a cell tagged as a CONSTANT or it is a cell previously investigated during the marking phase. An investigated cell either has its m-bit or f-bit set to TRUE. Any cell in a chain different from the head of the chain is called an internal cell.

In WAM an unbound variable is represented by a cell pointing to itself. Such a cell forms a chain by itself, in which case the head and the last cell of the chain coincide.

The following figure shows a chain starting from the stack and whose last cell is a constant. The arcs of the chain are marked 1,2,3,4.



Although cyclic structures do not normally occur in Prolog, we show here a chain starting from the second cell of a list and ending in a cell completing a cycle. The arcs of the chain are marked 1,2,3. Notice that the chain consists of four cells, the cell between arc 1 and 2 is both the second and last cell of the chain.

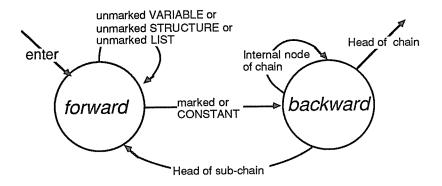


We are now ready to present the core of the marking algorithm, the procedure mark_variable. The following algorithm uses a new pointer reversal algorithm especially adapted for WAM data structures. An extra stack is thus unnecessary. Also it is capable of marking cells within structures, creating situations where part of the structure is collected as garbage and part of it is not. This is important since pointers into structures are quite frequent.

The algorithm is described by a finite-state machine with two states: forward and backward.

The forward phase traverses a chain of pointers which becomes reversed. During this phase when an unmarked structure or list is reached, a return pointer to the current chain is saved in the last cell of the structure. We then continue the forward phase with a sub-chain originating in this cell. Alternatively, if a constant or a marked cell is encountered, the backward phase is entered.

In the backward phase pointer reversal is undone until we return to the starting point denoted by the head of the current chain. If this cell is the starting point of the whole marking phase, we are finished. Otherwise, the cell is a component of a structure and the traversal continues in the forward mode with the previous component in the structure.

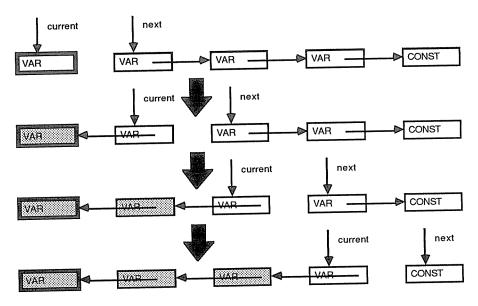


Two pointers for traversing the data structures are used during this phase: current and next. current points to the cell currently being processed, whereas next contains the original value of what current pointed to. The following is a detailed description of the two phases of the marking algorithm.

The Forward Phase

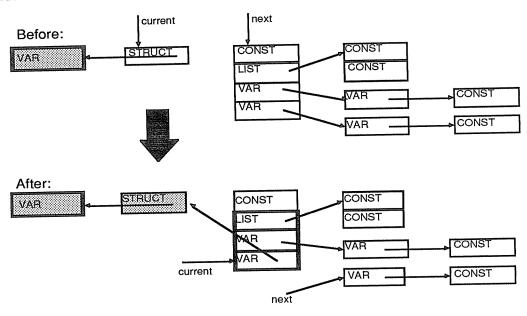
Initially current points to a stack cell which has its f-bit set, and next contains the value of that cell. Execution may then enter the forward phase:

1. If current points to an unmarked VARIABLE cell, we get the state transition depicted by the following figure where shaded cells denote cells having their m-bit set and bold outlined cells denote cells having their f-bit set. The f-bit is used to distinguish the "head of chain" from an internal cell. Note that the new current cell becomes marked as an internal cell. After the transition, execution continues in the forward mode. The figure below shows several such transitions.



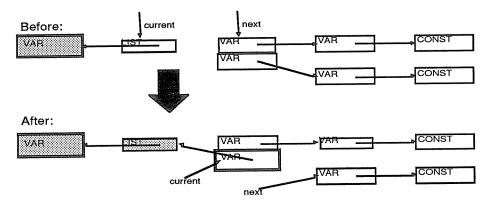
Transformation 1

2. If current points to an unmarked STRUCTURE or an unmarked LIST a fairly complicated transition takes place, as can be seen from the following figure. First the current cell is marked and all the components of the structure next points to are examined. If the second component has its f-bit set, the structure is already being traversed, and execution continues in the backward phase. Otherwise, the f-bit is set in all components but the first. This indicates that all these components are heads of sub-chains. Thereafter the pointers are arranged so that execution may continue in the forward mode with current pointing to the last cell of the structure.



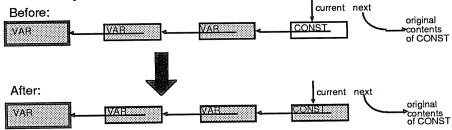
Transformation 2a

Below an example is given where current points to a list cell.



Transformation 2b

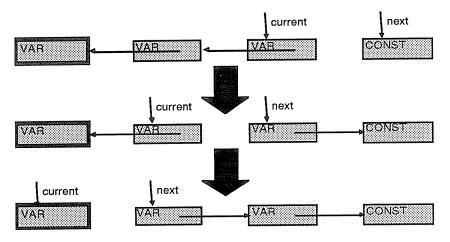
3. If current points to a marked cell or an unmarked CONSTANT cell, the current cell becomes marked if unmarked, and the backward phase is entered.



Transformation 3

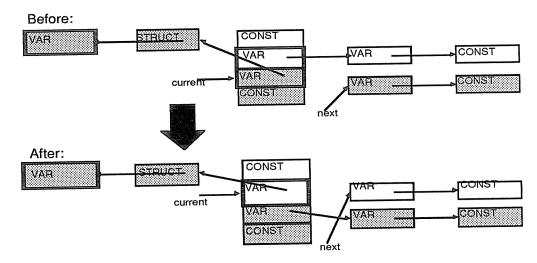
The backward phase

This phase resets the pointers of a chain to their original values. All internal cells are reversed until the "head of chain", which has its f-bit set, is encountered. Since the f-bit now has fulfilled its purpose (being the indicator for the "head of chain") it is reset.



Transformation 4

We have then either arrived at the starting cell of the call to mark_variable and the marking terminates, or it is a cell not being the first in a LIST or a STRUCTURE. In the latter case, as the cells of a structure are investigated from the last to the first, current is advanced to point to the previous cell. The pointers are then arranged so that execution may continue in the forward mode, see below.



Transformation 5

Before we are ready to show the code for the mark_variable procedure, some help-macros need to be defined. To simplify the definitions of those help-macros, a help-help-macro is first defined:

• Swap3(x,y,z) means temp=x; x=y; y=z; z=temp; The help-macros then get the following definitions:

- Reverse (current, next) means Swap3 (next->value, current, next)
- Undo (current, next) means Swap3 (current->value, next, current)
- Advance(current, next) means Swap3((current+1)->value, next, current->value)
- Lastcell(current, next) returns a pointer to the last component of the structure current points to. It may be necessary to use next for this calculation as it contains the original value of current->value, which contained the length of the structure. For a list, however, the address of the last component is always next+1.

During the marking, the number of marked cells is calculated by incrementing the variable total_marked. In order not to count the cells on the stack, total_marked is decremented at the start.

```
mark_variable(start)
         struct valuecell *start;
         struct valuecell *current, *next;
                 current = start;
                 next = current->value;
                 current->f = TRUE;
                 total_marked = total_marked-1; /* don't count stack cells */
                 goto forward;
         forward:if(current->m == TRUE) goto backward;
                 current->m = TRUE;
                 total marked = total marked+1;
                 switch(current->tag) {
                                            /* transformation 1 */
                 case VARIABLE:
                        if(next->f == TRUE)
                              goto backward;
                        Reverse (current, next);
                        goto forward;
```

```
case STRUCTURE:
                                  /* transformation 2a */
                                  /* transformation 2b */
       case LIST:
             if((next+1)->f == TRUE)
                    goto backward;
              /* setting the f-bits */
              for every cell in object referred by next,
              except the first component
                    set f bit TRUE;
              next = Lastcell(current, next);
              Reverse (current, next);
              goto forward;
                                  /* transformation 3 */
       case CONSTANT:
              goto backward;
        }
                                        /* transformation 4 */
backward:if(current->f == FALSE)
              { /* internal cell */
              Undo(current, next);
              goto backward;
              }
        /* head of chain */
        current->f = FALSE;
        if(current == start)
              return;
                                         /* transformation 5 */
        current = current-1;
        Advance (current, next);
        goto forward;
}
```

Optimizations of mark variable

Each time a object is marked, *all* its components are individually investigated, regardless of whether the object has been marked before or not. It is wrong to assume that the whole object has been marked if a single component has been marked, since individual components may be marked if they are referred from VAR-cells. Investigating all the components may be time consuming, although the algorithm is still linear in principle.

In order to speed up execution, we may check all of the cells to see if they are marked. The following code, inserted just before setting the f-bits of the components, will accomplish this:

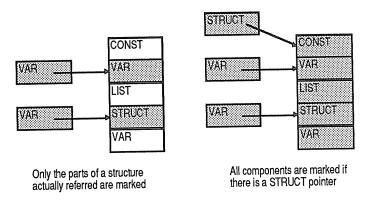
An even better solution is to use the observation that the first component of a *structure* may never be referred to directly from a VAR-cell, and thus may never be marked individually. Since the first cell is the last cell marked, it is sufficient to test this cell alone to know whether the structure as a whole has been marked. We then get the following piece of code which is inserted just before the setting of the f-bits:

```
if(current->tag == STRUCTURE AND next->m == TRUE)
    goto backward;
```

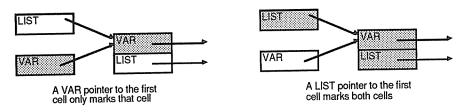
A corresponding optimization for LISTs is not possible as the first component may be reached directly from a VAR-cell.

Some extreme cases

It is not immediately obvious that the marking algorithm is able to handle quite complex structures. We have already mentioned the ability of the algorithm to mark only those *parts* of a structure that are actually referred to. If the rest of the structure remains unmarked, those cells will be reclaimed later.

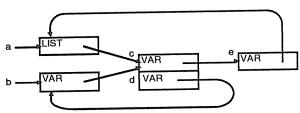


A variant of this is when the first cell of a list is also referred to from a VAR:



Although cyclic structures are seldom constructed in ordinary Prolog programs, in some applications they do occur. The marking algorithm handles them gracefully, without treating them separately. When a marked cell is encountered, the marking algorithm enters the backward mode.

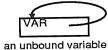
Extra care was taken when constructing the algorithm so that it would correctly handle cyclic structures like the one below.



If the marking starts with cell a, it will first come to the two cells c and d. Since a composite object is always scanned backwards, cell d will be investigated first. The reference from there leads to b and then back to c, which is still unmarked, although it is part of a structure being investigated. The marking continues with e and finally returns to a, which is marked so the backward mode is entered.

On the other hand, if marking instead starts with b, passing through c, e, a and back to c, a cycle will not be formed until c. Although c is marked, we do not enter the backward mode here since d has not yet been marked. A trace of the execution would show that the marking algorithm is able to handle both these cases.

A very special cyclic structure is an unbound variable. Usually, it is represented by a cell pointing to itself. The marking algorithm needs no special code for this case, although it might speed up execution.



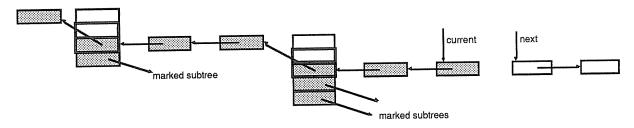
Informal correctness proof of the marking algorithm

It is guaranteed that the marking algorithm marks all reachable objects, resets all pointers to their original values and that it terminates. The main complexity of the algorithm lies in the procedure mark_variables. No correctness proof is given here, but a sketch looks like this:

The following preconditions for the forward and the backward phase are always maintained:

- next always contains the original value of current->value.
- current always points to a return-chain, where a return-chain is defined as follows: current is the end of a chain whose first cell has its f-bit set. This first cell is either the starting cell (start) or a component of a structure.

In the latter case, that component refers back to the STRUCTURE or LIST value cell which originally pointed to the structure. Now, that STRUCTURE or LIST cell is instead part of a return chain. All components with higher addresses are marked subtrees, as shown by the figure below. All lower components of the structure, besides the first, have their f-bits set.



A typical return-chain

For the backward phase, the following is also always true:

next points to a marked subtree.

The preconditions are easily shown to be true initially. By performing a case-analysis, it can be shown that they are maintained throughout the computation. If the computation terminates, it will end in the backward mode, with current being the root of the marking and next, i.e. current->value, pointing to a marked subtree.

It remains to show that the computation actually terminates. Once an object is encountered, it is always marked. If a marked object is found, the marking enters backward phase. As no two return-chains ever cross each other (thereby creating a loop) and there is only a finite number of cells, the computation must terminate.

The Compaction Phase

Our goal for the compaction phase was to find a linear algorithm that used no extra space. As in [Pittomvils 85] our algorithm is based on Morris' algorithm [Morris 78], adapted for the Prolog environment. The algorithm is of order n, requiring two passes through the heap, one pass through the trail, and one pass through the stack. The heap is scanned, once to update upward pointers and once to update downward pointers.

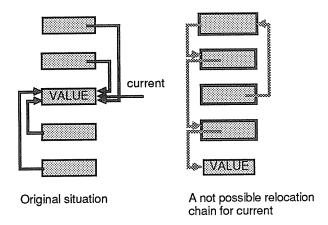
First the basic sweeping algorithm is described and then we make some additions to make it suitable for WAM.

Compacting the heap

By sweeping the heap from low to high addresses, having a destination pointer which is incremented for each marked object encountered, it is possible to know the final location of each object. Similarly, since we know how many value cells are marked, as calculated in total_marked, we can alternatively sweep the heap from high to low address. The main problem with the compaction phase is however not to calculate the final location of a certain cell, but to find and update all those cells pointing to this cell. A very natural solution would be to link all those value cells into a

relocation chain, which can be scanned when the final destination of the cell is known.

The first figure below shows all variable cells pointing to the cell current. In the second figure all those cells are linked into a chain starting at current and ending with a cell containing the original value of current.



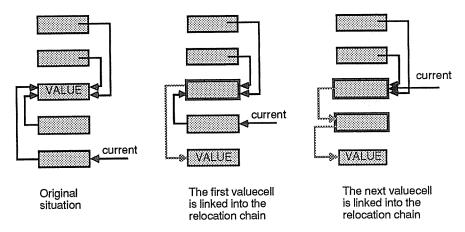
A moment of afterthought indicates however that this is not a possible solution. Many cells contain pointers and thus need to be part of a relocation chain, however at the same time they may be pointed to and thus need to be the head of another relocation chain!

Morris' algorithm elegantly solves this apparent contradiction by allowing some valuecells to be the head of relocation chains part of the time, and to be members of relocation chains part of the time. As mentioned previously, compaction consists of two phases, one upward sweep and one downward sweep.

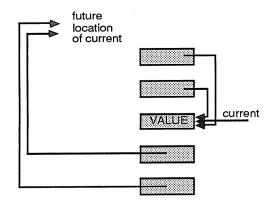
In the upward phase, the heap is scanned from high to low, and only marked valuecells pointing upwards are considered. Whenever such a cell is encountered, it is linked into the relocation chain of the cell it points to. The f-bit is used to indicate that a cell is in a relocation chain. As before, such cells are shown with a bold outline in our figures.

Each marked cell, regardless of its pointer value, is however first checked to see whether it is the head of such a chain. If so, all members of the chain are updated to point to the new location of the cell. In this process, the cell also regains its original value. If the original value points upwards, it must also be inserted into a relocation chain.

The figure below shows a series of situations during the upward phase as the pointer current passes through the heap.



current is now the head of a relocation chain whose members will be updated to contain the future location of current. In this process current also regains its original VALUE, see below.



The value of current is now inspected to see whether it is an upward pointer. If so, the cell is linked into the relocation chain of the object pointed to.

This is done by calling into relocation_chain(current->value, current).

Thereafter, current is advanced to point to the next marked valuecell. In this simple example the remaining value cells all point downward and nothing more will happen during the upward phase.

After the upward phase all valuecells pointing upwards have their final correct values.

The downward phase is almost a mirror image of the upward phase, scanning the heap in the opposite direction. The difference is that all marked valuecells, regardless of their contents, are moved to their new location and their m and f bits are reset. There is no danger that moving a cell will destroy any other cell, as the destination is always closer to the bottom of the heap than the source and all lower cells have already been moved.

The downward phase resets all downward pointers. Thus, the downward phase in combination with the upward phase assures that all pointers are correctly reset.

```
compact_heap()
struct valuecell *dest, *current;
/* the upward phase */
dest = heap low + total marked - 1;
for current = H down to heap_low
         if(current->m == TRUE)
                 update relocation chain (current, dest);
                 if(current->value is a heap pointer)
                       if(current->value < current)</pre>
                              into relocation_chain(current->value,current);
                       else if(current == current->value)
                              /* a cell pointing to itself */
                              current->value = dest;
                        }
                 dest = dest-1;
                 }
         }
/* the downward phase */
dest = heap_low;
for current = heap_low up to H
         if(current->m == TRUE)
                 update relocation_chain(current,dest);
                 if(current->value is a heap pointer AND
                        current->value > current)
                        {
                        /* move the current cell and insert it into
                              the relocation chain */
                        into relocation_chain(current->value, dest);
                        dest->tag = current->tag;
                        }
                 else
                        /* just move the current cell */
                        dest->value = current->value;
                        dest->tag = current->tag;
                        dest->f = FALSE;
                 dest->m = FALSE;
                 dest = dest+1;
```

```
}
         }
}
update_relocation_chain(current,dest)
struct valuecell *current, *dest;
{
         struct valuecell *j;
         while (current->f == TRUE)
                        j = current->value;
                        current->value = j->value;
                        current->f = j->f;
                        j->value = dest;
                        j->f = FALSE;
}
into relocation_chain(j,current)
struct valuecell *j, *current;
{
          current->value = j->value;
          current->f = j->f;
          j->value = current;
          j->f = TRUE;
}
```

Updating pointers from other data areas into the heap

As mentioned initially, the heap is not the only data area containing heap pointers. The stack, the trail and the argument registers A also refer to the heap and those pointers also have to be updated. By simply sweeping those areas looking for pointers into the heap and inserting those cells into the relocation chain, the compact_heap procedure will automatically update those references.

The main procedure for the compaction then becomes

```
compaction_phase()
    {
      push_registers();
      sweep_trail();
      sweep_stack();
      compact_heap();
      pop_registers();
    }
```

Sweeping the registers

The registers are temporarily pushed onto the trail so that they may be referred to from the heap. The updated registers are finally restored by pop_registers.

Sweeping the trail

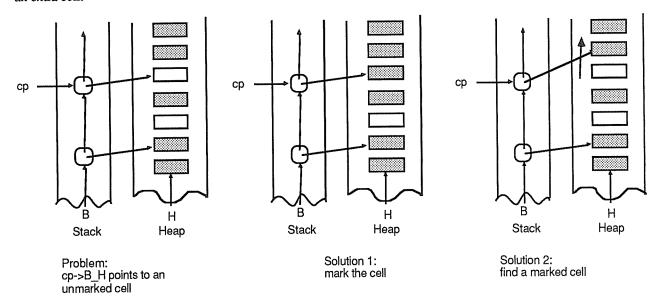
The procedure sweep_trail inserts the cells of the trail into the relocation chains. Note that the registers being pushed onto the trail will be handled here also.

Sweeping the stack

sweep_stack calls both sweep_environments and sweep_choicepoints in a manner very similar to the marking phase. One difference is that the m bits are reset during the traversal, so that upon completion all m bits are reset in the stack. If an unmarked variable is encountered in sweep_environments, the procedure returns immediately since that environment must already have been encountered.

Extra care has to be taken with the saved top-of-heap pointers in the choice points, i.e. the H component of a choice point. This pointer indicates how far to reset the top of heap on backtracking. Since the objects in the heap may move, it may also be necessary to update this pointer. It is not sufficient just to insert the H component into the relocation chain of the value cell referred because that cell may be unmarked. A simple and effective solution to this problem is simply to mark that cell and insert something harmless there, for instance NIL.

Alternatively, the heap may be searched until a marked object is found and then change the H component to point to that object instead. The advantage of the former solution is that no search is needed, whereas the latter avoids allocating an extra cell.



The best solution is probably a compromise, where the heap is searched for a limited number of cells, and only if no marked cell is found, is an unmarked cell then marked.

For simplicity, the code presented here uses the first alternative.

```
sweep_stack()
         sweep_environments(E,env_size(L));
         sweep choicepoints (B);
sweep_environments(env, size)
         struct environment *env;
         int size;
         {
         while (env #NULL)
                 for each v pointing to a valuecell in env->Y
                     scan the "size" number of cells from high to low
                        if(v->value points to the heap)
                              if(v->m == FALSE) /* we have already been here */
                                     return;
                              else
                                     v->m = FALSE;
                                     into_relocation_chain(v->value, v);
                  size = env_size(env->CL);
                  env = env->CE;
                  }
          }
sweep_choicepoints(cp)
          struct wam *cp;
          while(cp # NULL)
                  sweep_environments(cp->E,env_size(cp->L));
                  for each v pointing to a valuecell in cp->A do
                        if(v->value points to the heap)
                               v->m = FALSE;
                               into_relocation_chain(v->value, v);
                  if(cp->H->m == FALSE)
                              /* create a dummy constant on the heap */
                         cp->H->value = NIL;
                         cp->H->tag = CONSTANT;
                         cp->H->m = TRUE;
                         cp->H->f = FALSE;
                         total_marked = total_marked+1;
                   into_relocation_chain(cp->H, &(cp->H));
                   cp = cp -> B;
           }
```

As already mentioned, the notation & (cp->H) means the address of (cp->H).

Putting the pieces together

Having defined the marking and compaction phases, the basic garbage collection algorithm now becomes simply:

This concludes the basic garbage collection algorithm.

Optimizations of garbage collection for WAM

Early reset of variables

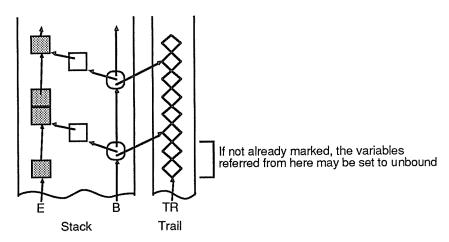
As shown by the following Prolog program, some data structures will be created which are not useful, but which will be marked anyway by the basic garbage collection algorithm.

```
test(B) :- p(A,B).
p(A,B) :- create_a_big_structure(A), q(B).
p(A,B) :- something(A), r(B).
```

If the query "?- test(B)." is posed, a choice point will be created for the second clause of p. Then create_a_big_structure(A) is called which sets A to refer to a very big structure. If A is not accessible through the active environment chain, this big structure is no longer needed when q(B) is called. However, from the choice point created, A is still reachable, and thus also the big structure.

How can the marking phase be modified to handle this situation?

Let us examine the marking code once again. First all argument registers and all environments reachable from the current environment are marked. Then all choice points and environments reachable from these choice points are marked. But some of those variables will be reset before we backtrack to the latest choice point! The solution seems to be to reset those variables, if they are unmarked, *now*, before marking the choice point.



The argument can be repeated for each choice point: unmarked variables referred to from trail entries younger than the choice point are reset before marking the choice point. This is possible to do as those variables are only reachable after backtracking, at which point they will be reset anyway.

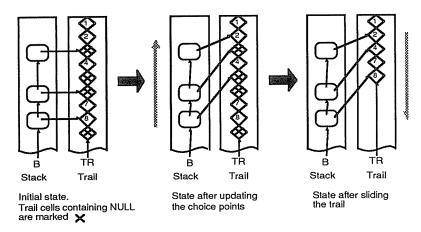
To implement the early reset of variables, mark choicepoints now becomes instead:

```
mark choicepoints(cp)
         struct wam *cp;
         struct valuecell
         t = T;
         trailcells_deleted =
         while(cp ≠ NULL)
                while(t > cp->T)
                      if((*t)->m ==
                                      FALSE)
                            {
                            reset(*t);
                            (*t) = NULL;
                            trailcells_deleted = trailcells_deleted+1;
                      t = t-1;
                mark environments(cp->E, env_size(cp->L));
                for each v pointing to a valuecell in cp->A do
                      mark_variable(v);
                cp = cp -> B;
         }
```

The procedure reset(x) sets the valuecell x to unbound. Trail entries pointing to variables being reset are set to NULL as they are no longer needed. Thus, these trail entries could be discarded and the trail compacted.

If this is done, entries in the trail will be moved and the corresponding pointers into the trail from the choice points have to be updated. The trail must be scanned from trail_low to T in order to compact the trail towards the lower addresses. Ideally, the choice points would be scanned and updated simultaneously. However, this is not possible as they are linked in the opposite direction.

One of many possible solutions to this problem is first to scan the choice points from high to low address updating the trail pointers T of the choicepoints, and then to compact the trail going from low to high address. When scanning the choice points, the trail cells are also scanned, decrementing the counter trailcells_deleted for each discarded trail entry. By subtracting the current value trailcells_deleted from the T field of the choice point visited, that field will contain the address of the relocated trail cell.



After mark_choicepoints has been called, the new procedure collect_trail is called which first updates the choice points and then compacts the trail.

```
update choicepoints();
         struct choicepoint *cp;
         struct valuecell **t;
         cp = B;
         t = T;
         while(cp ≠ NULL)
                 {
                 while(t > cp->T)
                        if((*t) == NULL)
                            trailcells deleted = trailcells deleted-1;
                        t = t-1;
                 cp->T = cp->T - trailcells_deleted;
                 cp = cp -> B;
          }
compact trail()
          ſ
         struct valuecell **dest, **current;
         dest = trail low;
         for current = trail low up to T
                 if((*current) ≠ NULL)
                        {
                        (*dest) = (*current);
                        dest = dest+1;
          T = dest-1;
```

A method closely related to early reset called *virtual backtracking* has previously been described by [Bekkers 83, Bruynooghe 84, Pittomvils 85]. However, in virtual backtracking the variables are not reset and the entries in the trail are not removed.

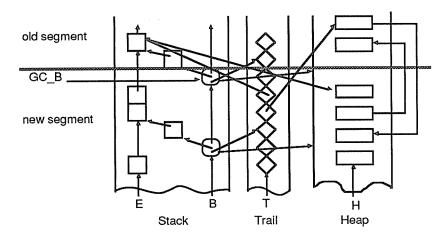
Segmented Garbage Collection

It is possible to divide the data areas of Prolog into segments for which garbage collection can be performed independently. When a choice point is created on the stack, all currently active argument registers are copied into that choice point, fixing all structures accessible from these variables. Structures in the heap that are not garbage at that moment will remain non-garbage until the choice point is removed upon backtracking. To take advantage of this we divide the main data areas into segments. A new segment is started in the stack, heap and trail after a choice point is placed on the stack. Only segments for which garbage collection has not been performed or segments that have been reopened upon backtracking need to be collected.

Segmented garbage collection can be implemented using one extra variable, GC_B, which points to the choice point ending the oldest segment for which garbage collection has been performed. When garbage collection is performed, GC_B is reset to the youngest choice point in the stack. During execution, when a choicepoint is removed, if B points to an older choice point than GC_B, GC_B is reset to B.

Alternatively, to avoid this overhead during execution, a special bit may be set in each choice point which has taken part in a garbage collection. GC_B then corresponds to the youngest choice point having this bit set. For simplicity, we ignore this optimization.

The figure below shows a typical situation during execution. The stack, trail and heap are divided into two segments, new and old, by the choice point referred to by GC B.



In order to make a correct marking, we need to find all pointers going from the old segment to the new segment. The only pointers of this kind are pointers from the stack or the heap to the heap. All those pointers may be found without scanning the whole old segment since they are always recorded on the trail as shown in the figure. This is guaranteed by the fact that there is at least one choice point, the GC_B choice point, which lies "between" the two cells. The unification algorithm always records such pointers on the trail, since they have to be reset upon backtracking.

Thus the marking phase only needs to examine the new segment and the cells in the old segment referred from the new trail.

However - and this is the only drawback of segmented garbage collection - some of the pointers going from the old heap to the new heap would normally be reset by the "early reset" mechanism described earlier. The segmentation mechanism prevents this since all value cells in the old segment are considered equally reachable, and we cannot know whether a certain cell on the old heap is reachable from the new segment. Thus "early reset" is disabled for the old segment.

Changes to the marking

A pointer P points to the old heap if $P \leq GC_B - > H$, it points to old stack if $P \leq GC_B$ and it points to the old trail if $P \leq GC_B - > T$. We get the following modifications of the marking phase:

```
In mark_environments the while-loop instead becomes

while (env \neq NULL AND env points to the new stack)
```

As mentioned, all pointers going from the old heap to the new heap are found on the new trail. Before calling mark choicepoints in the procedure marking_phase, the procedure mark_trail is called.

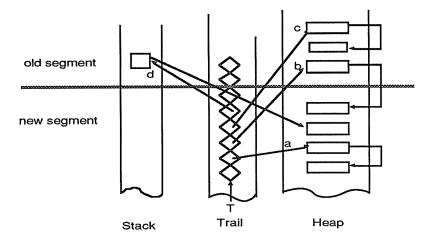
In mark_variable the test in the forward mode becomes

which reflects the idea that all objects in the old heap segment are to be considered marked, and should not be touched.

Changes to the compaction phase

Since only the new heap will be compacted, only pointers into the new heap need to be considered for updating. Thus, pointers to the old heap should not be considered. The test in the procedure push_registers therefore becomes if (A[i]->value points to the new heap)...

The procedure sweep_trail now only sweeps the *new* trail, putting all entries pointing to the new heap into the relocation chain as before (case a in the figure below). Trail entries pointing to the old segment do not need to be updated as the old segment will not be moved by compaction (cases b,c and d). However, if the old heap or stack cell refers to the new heap (cases b and d), that cell needs to be updated.



A modified version of sweep trail, that takes care of those special cases will now look like this

The modifications needed for sweep_environments and sweep_choicepoints are quite similar. By adding a test env points to the new stack and cp points to the new stack respectively to the main while-loops, only the new stack will be scanned. The tests for references to the heap are changed into tests for references to the new heap.

Discussion

It is interesting to compare our marking algorithm to Thorelli's [Thorelli 72], which also uses a pointer reversal technique not needing any extra storage for the traversal, besides one cell per object. This extra cell contains a counter indicating how far the object has been marked. If the largest object contains n cells, the counter must contain at least $\lceil \log_2 n \rceil$ bits. If many objects are close to the maximum object size Thorelli's method clearly becomes superior to our method where two bits are needed for each cell. However, most objects in Prolog are much smaller than the largest one. But the main reason for not using Thorelli's approach is that it does not seem possible to extend his scheme to mark just parts of an object.

In one of the first described garbage collection algorithms specifically for Prolog by Warren [Warren 77], the outer unmarked parts of an object may be freed, but not the inner unmarked parts surrounded by marked cells. This limitation seems inherent in implementations based on "structure sharing".

A source of inspiration for our work has been the series of publications by Bruynooghe [Bruynooghe 82, Bruynooghe 82B, Bruynooghe 84] leading to [Pittomvils 85] where the ideas of virtual backtracking [Bekkers 83] and segmented garbage collection [Lieberman 83] have been incorporated.

The main novel result of this paper is the marking algorithm, which needs only two bits per word and no extra stack space. It also has the capability of marking only the parts of a structure that are reachable.

Another novelty is the concept of "early reset of variables", instead of virtual backtracking. By resetting a variable ("early reset"), instead of indicating that what it points to should not be marked ("virtual backtracking"), we are able to compact the trail, as some trail entries are no longer needed.

The paper gives a fairly detailed description of how to implement the various parts of the garbage collection algorithm, including how to adapt it to segmented garbage collection.

The compaction algorithm presented here is proportional to the size of the heap, not to the number of reachable objects. Given a program which generates a lot of garbage, a significant amount of time may be spent in the compaction phase. Adding a new phase inserted between marking and compaction which links the marked objects using the unmarked objects as link-nodes, would enable the compaction phase to just scan the marked cells. Such an intermediate phase can be made proportional to $n \log n$, where n is the number of marked cells [Sahlin 87].

The question of completeness naturally arises, i.e. does the algorithm find and deallocate all garbage. For deterministic languages the question is easy to answer, but for a nondeterministic language it becomes more complex since the machine contains many frozen states. Without giving a proof we claim the garbage collection algorithm presented (with "early reset" but without segmentation) is complete in the following sense: Assume that we had a WAM-machine that could "fork" itself at each choice point. Each machine would then execute deterministically, not having any choice points at all. A set of such machines corresponds to the state of an ordinary WAM-machine having choicepoints. The objects reachable in all these machines correspond exactly to those objects we consider reachable in our algorithm.

This does not mean however that we have reclaimed all possible storage. The "single assignment" property of Prolog makes more semantical optimizations possible. For instance, chains of variables may be collapsed, making it possible to deallocate the intermediate cells and thus also later speed up execution.

Another storage optimization would be to find objects of exactly the same structure and collapse all these objects into one canonical representative. By having a special "canonical" bit in the pointer to those objects, the unification of two such objects just becomes a pointer comparison. Finding all equal objects is possibly too time-consuming for this optimization to be worth-while, but this remains to be investigated.

Acknowledgements

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Bibliography

[Barklund 86]	J. Barklund, H. Millroth, "Garbage Cut for Garbage Collection of Iterative Prolog Programs", Proc. 1986 Symposium on Logic Programming.
[Bekkers 83]	Y. Bekkers, B. Canet, O. Ridoux, L. Ungaro, "A Short Note on Garbage Collection in Prolog Interpreters", Logic Programming Newsletter, no. 5, Winter 83/84
[Bruynooghe 82]	M. Bruynooghe, "A note on garbage collection in Prolog interpreters", Proc. First International Logic Programming Conference, 1982, pp. 52-55
[Bruynooghe 82B]	M. Bruynooghe, "The Memory management of Prolog implementations", Logic Programming, Eds. K.L. Clark & S-Å Tärnlund, Academic Press, 1982, pp. 82-98.
[Bruynooghe 84]	M. Bruynooghe, "Garbage collection in Prolog interpreters", Implementations of PROLOG, ed. J. Campbell, Ellis Horwood, 1984, pp. 259-267.
[Carlsson 86]	M. Carlsson, "Compilation for Tricia and its Abstract Machine", Technical Report No. 35, 1986, UPMAIL, Uppsala University
[Gabriel 84]	J. Gabriel, T. Lindholm, E.L. Lusk, R.A. Overbeek, "Tutorial on the Warren Abstract Machine for Computational Logic", ANL-84-84, Argonne National Lab., Argonne, IL
[Lieberman 83]	H. Lieberman, C.Hewitt, "A real time garbage collector based on the life time of objects", CACM 26(6) (june 1983), pp. 419-429
[Morris 78]	F.L. Morris, "A time and space efficient garbage compaction algorithm", CACM 21(8) (Aug. 1978), pp. 662-665.
[Sahlin 86]	D. Sahlin, "Garbage collection using the reset information & Making tests deterministic using the reset information", March 1986, SICS working document.
[Sahlin 87]	D. Sahlin, "Making the garbage collection independent of the amount of garbage", SICS R87008 Research Report, ISSN 0283-3638
[Thorelli 72]	L-E Thorelli, "Marking Algorithms", BIT 12, 4, pp. 555-568, 1972
[Pittomvils 85]	E. Pittomvils, M. Bruynooghe, Y.D. Willems, "Towards a real time garbage collector for Prolog", Proc. Symposium on Logic Programming, 1985, pp. 185-198.
[Warren 83]	D.H.D. Warren, "An Abstract Prolog Instruction Set", Technical Note 309, SRI International, Menlo Park, CA, Oct. 1983
[Warren 77]	D.H.D. Warren, "Implementing Prolog – Compiling Predicate Logic Programs", University of Edinburgh Department of Artificial Intelligence Report 39 and Report 40, May 1977
[WarrenDS 84]	D.S. Warren, "The Runtime Environment for a Prolog Compiler Using a Copy Algorithm", SUNY at Stony Brook, NY, Technical Report #83/052